Six closely related YbT₂Zn₂₀ (T = Fe, Co, Ru, Rh, Os, Ir) heavy fermion compounds with large local moment degeneracy.

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Abstract

Heavy fermion compounds represent one of the most strongly correlated forms of electronic matter and give rise to low temperature states that range from small moment ordering to exotic superconductivity, both of which are often in close proximity to quantum critical points. These strong electronic correlations are associated with the transfer of entropy from the local moment degrees of freedom to the conduction electrons, and, as such, are intimately related to the low temperature degeneracy of the (originally) moment bearing ion. Here we report the discovery of six closely related Yb-based heavy fermion compounds, YbT₂Zn₂₀, that are members of the larger family of dilute rare earth bearing compounds: RT_2Zn_{20} (T = Fe, Co, Ru, Rh, Os, Ir). This discovery doubles the total number of Yb-based heavy fermion materials. Given these compounds' dilute nature, systematic changes in T only weakly perturb the Yb site and allow for insight into the effects of degeneracy on the thermodynamic and transport properties of these model correlated electron systems.

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Heavy fermion compounds have been recognized as one of the premier examples of strongly correlated electron behavior for several decades. Ce- and U-based heavy fermion compounds have been well studied, and in recent years a small number of Yb-based heavy fermions have been identified as well.[1] Unfortunately, in part due to the somewhat unpredictable nature of 4f ion hybridization with the conduction electrons, it has been difficult to find closely related (e.g. structurally) heavy fermion compounds, other than of the ThCr₂Si₂ structure, especially Yb-based ones, that allow for systematic studies of the Yb ion degeneracy. Part of this difficulty is associated with the fact that the 4f hybridization depends so strongly on the local environment of the rare earth ion.

Dilute, rare earth (R) bearing, intermetallic compounds are ordered materials with less than 5 atomic percent rare earth fully occupying a unique crystallographic site. Such materials offer the possibility of investigating the interaction between conduction electrons and 4f electrons in fully ordered compounds for relatively low concentrations of rare earths. For the case of R = Yb or Ce these materials offer the possibility of preserving low temperature, coherent effects while more closely approximating the single ion Kondo impurity limit. A very promising example of such compounds is derived from the the family of RT_2Zn_{20} [2] (T = transition metal) which has recently been shown to allow for the tuning of the non-magnetic R = Y and Lu members to exceedingly close to the Stoner limit as well as allowing for the study of the effects of such a highly polarizable background on local moment magnetic ordering for R = Gd. [3]

In this letter we present thermodynamic and transport data on six, new, strongly correlated Yb-based intermetallic compounds found in the RT_2Zn_{20} family for T = Fe, Co, Ru, Rh, Os, and Ir, effectively doubling the number of known Yb-based heavy fermions (compounds with linear coefficient of specific heat, γ , greater than 400 mJ/mol K^2 [1]). The RT_2Zn_{20} compounds crystallize in the cubic $CeCr_2Al_{20}$ ($Fd\bar{3}m$ space group) structure. [4, 5] Due to the relatively low concentration of rare earth, as well as transition metal, in these compounds, the four nearest neighbors as well as the twelve next-nearest neighbors of the rare earth ion are Zn atoms. The rare earth ion is coordinated by a 16 atom Frank - Kasper polyhedron and has a cubic point symmetry. This near spherical distribution of neighboring Zn atoms gives rise to the possibility of relatively low crystal-electric-field (CEF) split levels and also promises a large degree of similarity between this isostructural group of Yb-based heavy fermions. These compounds, then not only greatly expand the number of known Yb-

based heavy fermions, but, as will be shown below, also provide a route to studying how the degeneracy of the Yb-ion at Kondo temperature, T_K , effects the low temperature correlated state.

Thermodynamic and transport data taken on the six YbT₂Zn₂₀ compounds are presented in figures 1-3 and are summarized in table 1. Whereas the temperature dependent magnetic susceptibility, electrical resistivity and specific heat for T = Fe, Ru, Rh, Os, Ir are qualitatively similar, YbCo₂Zn₂₀ is, at first glance, somewhat different. Most conspicuously, instead of manifesting a clear loss of local moment behavior at low temperature,[6] the temperature dependent susceptibility continues to be Curie-Weiss-like down to 2 K (fig. 1a, inset).

Focusing initially on the five, apparently similar YbT₂Zn₂₀ compounds (for T = Fe, Ru, Rh, Os, Ir), figures 1a,b demonstrate that each of these compounds appears to be an excellent example of a Yb-based heavy fermion with electronic specific heat, γ , values ranging between 500 and 800 mJ/mole K². (The modest rise in the $\Delta C(T)/T$ data below 2 K is most probably associated with a nuclear Schottky anomaly and, for this work, is simply ignored. This assumption is further supported by the data and analysis presented in Fig. 5 below.) The low temperature magnetic susceptibility correlates well with the electronic specific heat values leading to the Wilson ratio (WR) [1] for these five compounds having values of 1.1 and 1.3 (see table 1). The temperature dependent electrical resistivity data (fig. 2) for these five compounds are also remarkably similar at high temperature and manifest clear T^2 temperature dependencies at low temperatures (see inset). Although resistivity data were taken down to 20 mK, no indications of either magnetic order or superconductivity were found for any of the YbT₂Zn₂₀ compounds.

The thermodynamic and transport properties of YbCo₂Zn₂₀ are somewhat different from the other five compounds. YbCo₂Zn₂₀ does not manifest the clear loss of local moment behavior, above 1.8 K, in the susceptibility data (see fig. 1a, inset) and the electrical resistivity and the specific heat only manifest Fermi liquid behavior for $T \leq 0.2$ K (fig. 3). Although the higher temperature electrical resistivity of YbCo₂Zn₂₀ is similar to the other five YbT₂Zn₂₀ compounds, it manifests a much clearer example of a resistance minimum and lower temperature coherence peak.

Some of the salient parameters extracted from these data are summarized in Table 1 and the coefficient of the T^2 resistivity (A) is plotted as a function of the linear coefficient of the specific heat (γ) in a Kadowaki-Woods (KW) [7, 8] type plot (fig. 4). Perhaps

the most noteworthy point that becomes clear from this presentation of the data is that, whereas there is relatively little variation in the low temperature thermodynamic properties, or Wilson ratio, associated with the T = Fe, Ru, Rh, Os, Ir compounds, there is an order of magnitude variation in the value of the coefficient of the T^2 resistivity, A. This gives rise to a vertical spread of the KW data points.

Recent theoretical work [9, 17, 18] has generalized the idea of a fixed KW ratio to one that can vary by over an order of magnitude, depending upon the value of the degeneracy of the Yb ion when it hybridizes. Figure 4 shows, as solid lines, the four degeneracies possible for the Kramers, Yb⁺³ ion. The YbT₂Zn₂₀ data indicate that for T = Fe, Ru the Yb ion has a significantly larger degeneracy upon entering the Kondo-screened state than it does for the T = Rh, Os, Ir compounds. The data point for YbCo₂Zn₂₀ approaches the far extreme of the KW plot, being near to the point associated with the exceptionally heavy fermion, YbBiPt. [10, 11]

As mentioned above, the sole Yb site is one of cubic point symmetery and is surrounded only by Zn in a shell of very high coordination number. Based on these facts it is anticipated that the Yb ion's Hund's rule, ground state multiplet will split into a quartet and two doublet states with a small total splitting. If indeed the difference between YbFe₂Zn₂₀ and YbRu₂Zn₂₀ on one hand and YbRh₂Zn₂₀, YbOs₂Zn₂₀ and YbIr₂Zn₂₀ on the other is the degree to which the Hund's rule ground state degeneracy has been lifted by crystalline electric field splitting before the Kondo screening takes place, then there should be some indication of this in other data as well. If, as Tsujii et al. suggest in ref. [9], the ratio of T_K to T_{CEF} is of primary concern, then an examination of figure 1a in the light of the Coqblin-Schrieffer model [6, 19], specifically figure 1 of ref. [6], indicates that the larger the ratio of the maximum susceptibility to the low temperature susceptibility, the larger is the degeneracy that remains in the Yb system at T_K . The ratios of the maximum susceptibility to the low temperature susceptibility to the low temperature susceptibility for T = Fe and Ru are 1.12 and 1.11 respectively whereas the ratios for T = Rh, Os, Ir are 1.06, 1.01 and 1.01, respectively. These values are consistent with a difference in degeneracy of at least $\Delta N = 2$ (see Fig. 4).

This analysis can be made even more thoroughly by performing a fit [6] to the magnetic component of the specific heat as well as the magnetic susceptibility over a wide temperature range. This is shown in figure 5 for YbFe₂Zn₂₀, the compound with the largest degeneracy inferred from the KW plot (Fig. 4) as well as from the above analysis. Both data sets are

best fit (and very well fit) by the J=7/2 (N=8) curves. The specific heat data is, in particular, most compelling since the height of the anomaly is not an adjustable parameter once N is chosen. This analysis further confirms the degeneracy inferred from figure 4. The inset to figure 5a shows the magnetic entropy as a function of temperature. By 60 K it rises past the J=5/2 value. The fact that it does not reach the $R \ln 8$ anticipated is most likely due to (i) difficulties in accurately modelling the non-magnetic contribution with LuFe₂Zn₂₀ at high temperatures and (ii) difficulties associated with taking the difference between two large, comparable values, as well as the fact that by 60 K a recovery of the full $R \ln 8$ is not expected (see fit to J=7/2 in main figure).

Given the above analyses, Figure 4 can be used to infer approximate degeneracies for the Yb ion in these YbT₂Zn₂₀ compounds (see Table I). We can then infer a value of T_K by using $T_K = (R \ln N)/\gamma$ [20] or by using $T_K = (N-1)\pi^2 R w_N/3N\gamma$ (where w_N is a multiplicative factor which is a function of N as discussed in [19]). These expressions produce T_K values that are within 5% of each other for $2 \le N \le 8$. It should also be noted that the T_K value estimated by this method is close to that found by fitting the whole C_p and χ curves (see Fig. 5 above). As could be anticipated, T_K values for T = Fe and Ru are indeed larger than those found for T = Rh, Os, Ir.

Given that our earlier work on the RT_2Zn_{20} families has shown that T = Fe and Ru compounds manifest anomalously high temperature, local moment ordering due to the fact that the Y and Lu host materials are close to the Stoner limit,[3] it is noteworthy that for the YbT₂Zn₂₀ materials it is the T = Fe and Ru compounds that appear to be significantly different from the T = Rh, Os, and Ir compounds. Although we currently do not have enough data to conclude that this Stoner enhancement of the host material (if it even persists in the Yb based members) is responsible for the higher T_K/T_{CEF} ratio, such an enhancement certainly could be responsible for increased T_K values. This question is the focus of an ongoing dilution study.

Although at first glance the data for YbCo₂Zn₂₀ appear to be different from that of the other members of this family, at low enough temperatures, it too appears to enter into a Fermi liquid ground state and, as shown in Fig. 4, has an intermediate N value, similar to YbOs₂Zn₂₀. YbCo₂Zn₂₀ has a substantially lower T_K , and may be closer to a quantum critical point than the other, T = Fe, Ru, Rh, Os, Ir members of the family. If YbCo₂Zn₂₀ is simply closer to a QCP, then, given that the unit cell dimensions for YbCo₂Zn₂₀ are

the smallest of the family, this would imply that applications of modest pressure to other members of the YbT_2Zn_{20} family may lead to several new Yb-based compounds for the study of quantum criticality.

Methods

Single crystalline samples of YbT₂Zn₂₀ were grown out of excess Zn using standard solution growth techniques. [21] Initial ratios of starting elements (Yb:T:Zn) were 2:4:96 (T = Fe, Co), 2:2:96 (T = Ru, Rh), 1:0.5:98.5 (T = Os), and 0.75:1.5:97.75 (T = Ir). Crystals were grown by slowly cooling the melt between 1150° C and 600° C over approximately 100 hours. In order to reduce the amount of Zn transported to the top of the growth ampoule, all growths were sealed under approximately 1/3 atmosphere of high purity Ar and were also slightly elevated from the hearth plate so as to insure that the top of the ampoule was slightly hotter than the bottom. Residual Zn flux was etched from the surface of the crystals using diluted HCl (0.5 volume percent, T = Fe, Co) or acetic acid (1 volume percent, T = Ru, Rh, Os, Ir). As can be seen in Figure 1, there is virtually no low-temperature Curie tail observed in any of the T = Fe, Ru, Rh, Os, Ir compounds, indicating little, or no local-moment-bearing impurities.

Magnetization measurements were performed for $T \geq 1.8$ K in a Quantum Design MPMS unit with the applied magnetic field along the [111] crystallographic direction. Specific heat and transport measurements for $T \geq 0.4$ K were performed in a Quantum Design PPMS system. Specific heat, C(T), data for 50 mK $\leq T \leq 2$ K were taken on YbCo₂Zn₂₀ in a dilution refrigerator insert for the Quantum Design PPMS system. Whereas all RT₂Zn₂₀ (R = Yb, Lu, Y; T = Fe, Co, Ru, Rh, Os, Ir) had Θ_D values near 255 K, the linear component of the C(T) was low (50 mJ/mol K² or less) [3] for the Lu- and Y- analogues and greatly enhanced for the Yb-bearing materials. Transport data were taken for T down to 20 mK at the NHMFL, Tallahassee using an Oxford dilution refrigerator. Powder X-ray diffraction measurements were performed on a Rigaku Miniflex unit. The YbT₂Zn₂₀ (T = Fe, Co, Ru, and Rh) compounds had diffraction patterns and lattice parameters that agreed well with the data for the RT₂Zn₂₀ series presented in ref. [2]. Although there are no prior reports on the ROs₂Zn₂₀ and RIr₂Zn₂₀ series, the diffraction patterns for YbOs₂Zn₂₀ and YbIr₂Zn₂₀ were easily indexed to the RT₂Zn₂₀ structure type. Room temperature unit cell parameters

are given in table 1.

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Competing interests statement:

The authors declare that they have no competing financial interests.

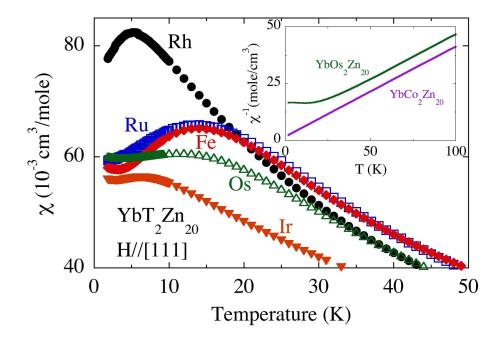
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TABLE I: Summary of structural, thermodynamic and transport data on YbT₂Zn₂₀ compounds (T = Fe, Co, Ru, Rh, Os, Ir) showing cubic lattice parameter, a; paramagnetic Curie-Weiss temperature, Θ , and effective moment, μ_{eff} , obtained from high temperature inverse susceptibility fit; low temperature magnetic susceptibility, χ_0 taken at 1.8 K; magnetic susceptibility at the maximum, χ_{max} and corresponding temperature, $T_{\chi_{max}}$; residual resistivity, ρ_0 , taken at $T \sim 20$ mK; coefficient of the T^2 resistivity, A(with range of fit given below); residual resistivity ratio, RRR; linear coefficient of the specific heat, γ ; Wilson ratio, WR; Kadowaki-Woods ratio, KWR; degeneracy, N; and estimated Kondo temperature, T_K .

Т	a	Θ	μ_{eff}	χ_0	χ_{max}	$T_{\chi_{max}}$	$ ho_0$	A	RRR	γ	WR	KWR	N	T_K
	Å	К	μ_B	$\frac{10^{-3}cm^3}{mole}$	$\frac{10^{-3}cm^3}{mole}$	K	$\mu\Omega$ cm	$\frac{\mu\Omega_{-}cm}{K^2}$		$\frac{mJ}{mol\ K^2}$		$\frac{\mu\Omega \ cm \ mole^2 \ K^2}{mJ^2}$		K
Fe	14.062	-24.5	4.8	58.0	65.1	14.0	2.1	$5.4\cdot10^{-2}$	31.2	520	1.2	$2.0\cdot10^{-7}$	8	33
								$(T \le 11 \text{ K})$						
Со	14.005	-5.6	4.5	415.1			21	165	2.8	7900		$27 \cdot 10^{-7}$	4	1.5
								$(T \leq 0.2~\mathrm{K})$						
Ru	14.193	-18.5	4.6	58.9	65.4	13.5	5.3	$6.8\cdot10^{-2}$	10.9	580	1.1	$2.0\cdot 10^{-7}$	8	30
								$(T \le 11 \text{ K})$						
Rh	14.150	-10.0	4.2	77.7	82.4	5.3	5.6	$54 \cdot 10^{-2}$	11.8	740	1.3	$10.1\cdot10^{-7}$	6	20
								$(T \le 6 \text{ K})$						
Os	14.205	-17.8	4.5	60.0	60.7	11.5	17	$53\cdot 10^{-2}$	4.4	580	1.1	$15\cdot 10^{-7}$	4	20
								$(T \le 1 \text{ K})$						
Ir	14.165	-24.2	4.4	55.9	56.3	6.5	8.8	$33\cdot 10^{-2}$	8.9	540	1.2	$11 \cdot 10^{-7}$	4	21
								$(T \le 5 \text{ K})$						



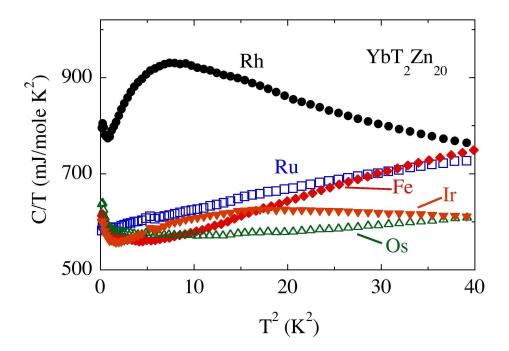


FIG. 1: Low temperature thermodynamic properties of YbT₂Zn₂₀ compounds (T = Fe, Ru, Rh, Os, Ir): (a) Magnetic susceptibility (H = 0.1 T). Inset: Temperature dependent inverse susceptibility for YbCo₂Zn₂₀ and YbOs₂Zn₂₀. (b)Low temperature specific heat, C, divided by temperature, as a function of T^2 .

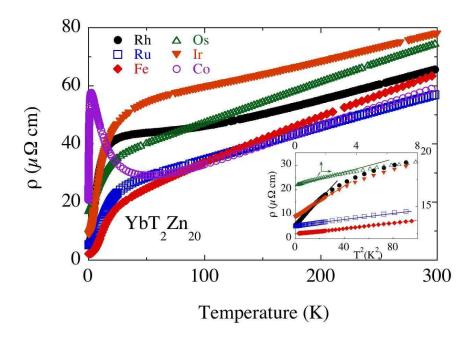


FIG. 2: Temperature dependent electrical resistivity of YbT_2Zn_{20} compounds (T = Fe, Co, Ru, Rh, Os, Ir). Inset: Low temperature electrical resistivity as a function of T^2 for T = Fe, Ru, Rh, Os, Ir; note separate axes for T = Os on top and right.

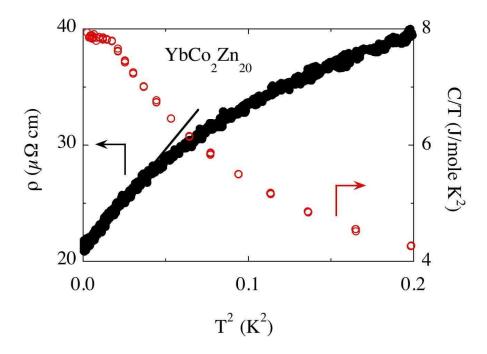


FIG. 3: Low temperature electrical resistivity and C/T of $\mathbf{YbCo_2Zn_{20}}$ as a function of T^2 .

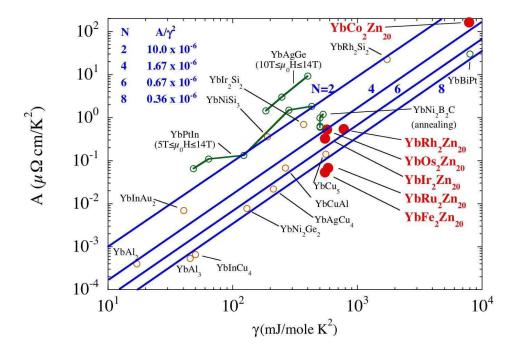


FIG. 4: Log-log plot of A versus γ (Kadowaki-Woods plot) of six new YbT₂Zn₂₀ heavy fermion compounds (T = Fe, Co, Ru, Rh, Os, Ir) shown with representative data from [9] as well as data for YbBiPt,[10, 11] YbNi₂B₂C,[12] YbPtIn,[13] YbAgGe,[14] YbNiSi₃,[15] and YbIr₂Si₂.[16] The solid lines for degeneracies N = 2, 4, 6, and 8 are taken from ref. [9].

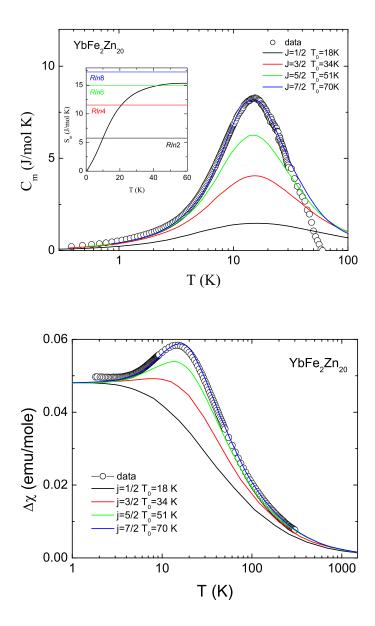


FIG. 5: Coqblin-Schrieffer analysis of thermodynamic data from YbFe₂Zn₂₀ after subtraction data from the non-magnetic analogue, LuFe₂Zn₂₀: (a) Magnetic specific heat and (b) Net magnetic susceptibility of YbFe₂Zn₂₀ as a function of temperature. Data are shown as open symbol and best fits to J = 1/2, 3/2, 5/2 and 7/2 using formalism described in [6] shown in black, red, green and blue lines respectively. T_0 values were determined by forcing C_p curves have maxima at the same location as the C_p data. The Kondo temperature that can be inferred from $T_0 = 70$ K and J = 7/2 is ≈ 37 K.